

# Challenges in fluid flow simulations using Exa-scale computing

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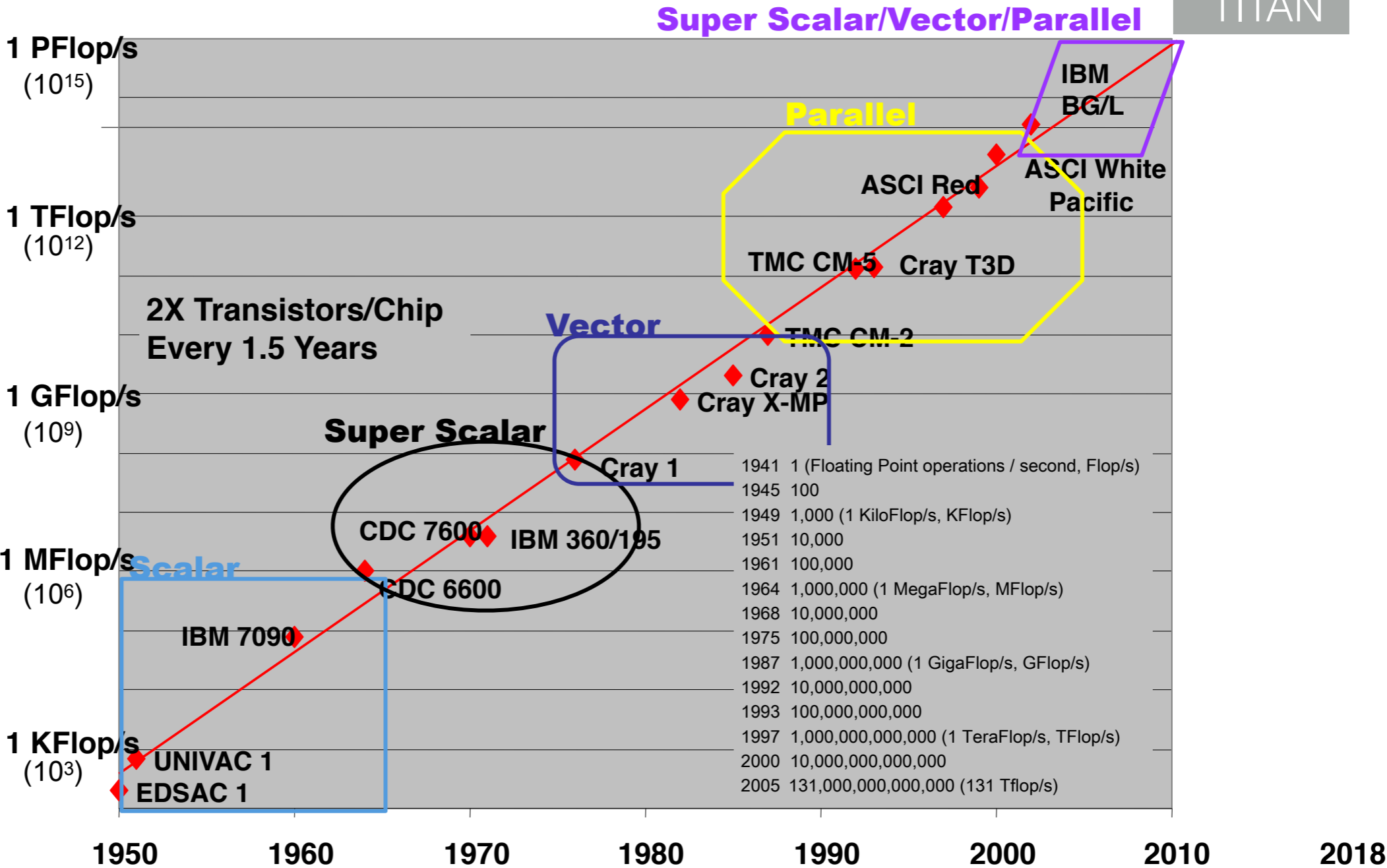


Hardware

# From Karniakadis's course slides

A Growth-Factor of a Billion in Performance in a Career

10<sup>18</sup>  
200 PF  
TITAN



# AMD EPYC™ 7551

## – Specifications

**# of CPU Cores:** 32

**# of Threads:** 64

**Base Clock:** 2GHz

**Max Boost Clock:** 3GHz

**All Core Boost Speed:** 2.55GHz

**Total L3 Cache:** 64MB

**Socket Count:** 1P/2P

**PCI Express Version:** x128

**Default TDP / TDP:** 180W

## – System Memory

**System Memory  
Specification:**  
2666MHz

**Memory Channels:** 8

**Mem BW (2S Theo):** 341 GB/s

<https://www.amd.com/en/products/cpu/amd-epyc-7551>

NODE: 2 proc/node; Focus on a node

Flop rating for 2 procs:  $2 * 32 * 24 = 1536$  GF

Wants data ~ 8 TB/sec.

Cache, RAM, HD

# Data transfer

FLOPS free, data transfer expensive (Saday)

Memory BW = 341 GB/s

SSD: transfer rate = 6 Gbit/s

peak IB Switch speed/port = 200 Gb/s

software challenges

# For beginners

- Abundance (MPI, OpenMP, CUDA, ML)
- Leads to confusion and non-start..
- Structured programming
- Pressure to do the science..
- Some times CS tools are too complex to be practical.



# For advanced users

- Optimised use of hardware.
- Structured and modular, usable code with documentation.
- Keeping up with upgrades and abundance (MPI3, ML, C++11, Vector processors, GPU, XeonPhi, Raspberry Pi).
- Optimization
- Interactions with users + programmers

Now CFD  
(Computational fluid  
dynamics)

# Applications

- Weather prediction and climate modelling
- Aeroplane and cars (transport)
- defence / offences
- Turbines, dams, water management
- Astrophysical flows
- Theoretical understanding

# Field reversal

with Mani Chandra

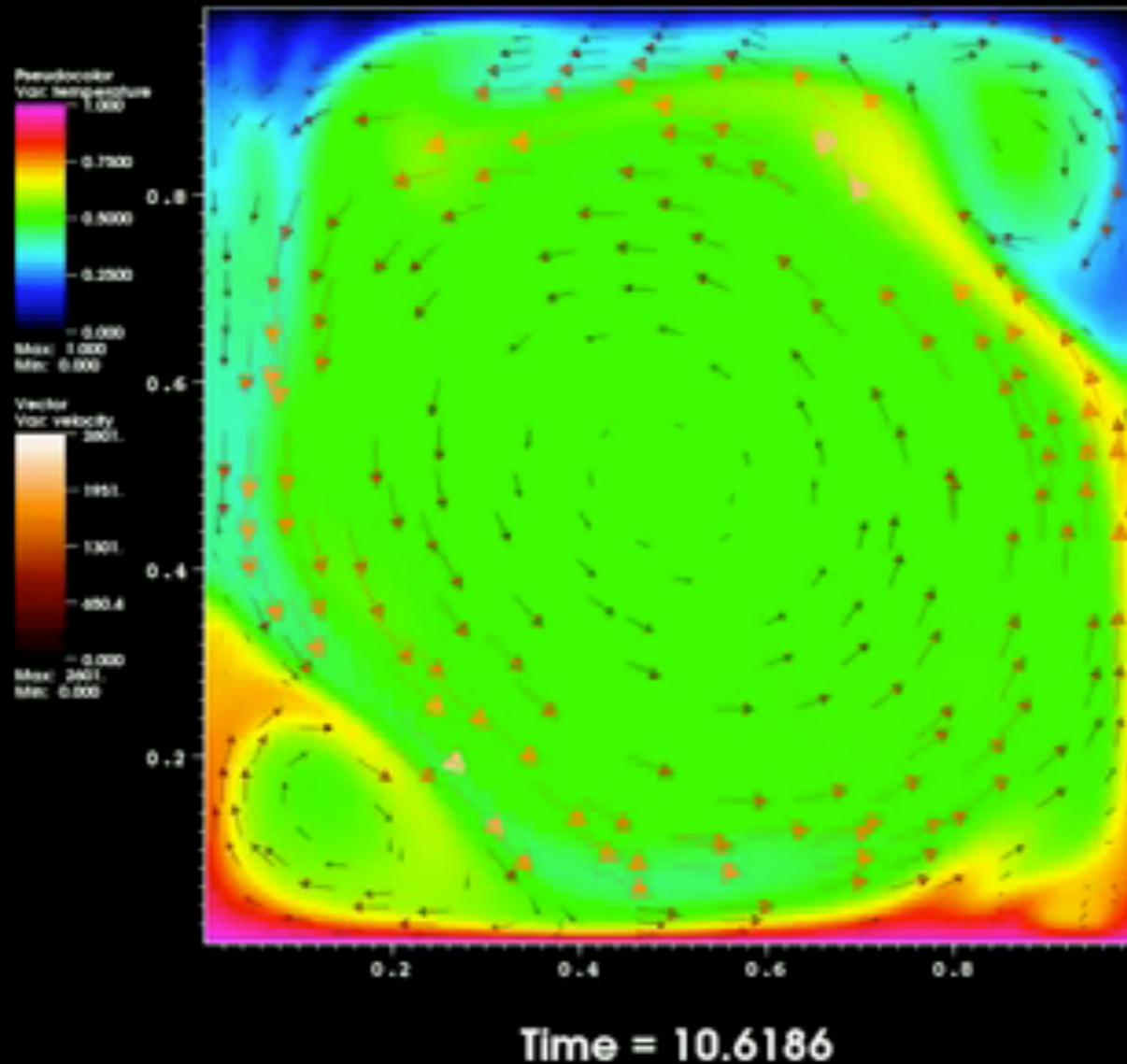
# Geomagnetism

Glatzmaier & Roberts  
Nature, 1995

Polarity reversals after  
random time intervals  
(tens of millions of  
years to 50K years).

Last reversal took  
place around 780,000  
years ago.

# Nek5000 (Spectral-element) simulation



$(1,1) \rightarrow (2,2) \rightarrow (1,1)$

spectral-element code  
Nek5000

Chandra & Verma, PRE 2011, PRL 2013

# Methods

- Finite difference
- Finite volume
- Finite element
- Spectral
- Spectral element

# Spectral method



# Example: Fluid solver

velocity  
field

Pressure

Ext. Force

$$\partial_t \mathbf{u} + (\mathbf{u} \cdot \nabla) \mathbf{u} = -\nabla p + \nu \nabla^2 \mathbf{u} + \mathbf{F}$$

$$\nabla \cdot \mathbf{u} = 0$$

Incompressibility

kinematic  
viscosity

$$\text{Reynolds no} = \frac{UL}{\nu}$$

Procedure

$$f(x) = \sum_{k_x} \hat{f}(k_x) \exp[i(k_x x)]$$

$$df(x) / dx = \sum_{k_x} [ik_x \hat{f}(k_x)] \exp[i(k_x x)]$$

Set of ODEs

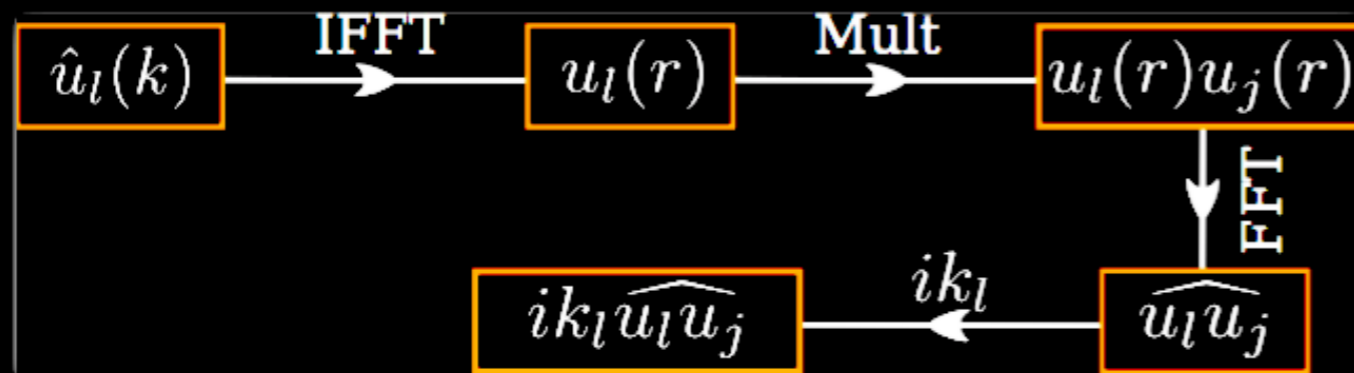
$$\frac{du_i(\mathbf{k})}{dt} = -jk_m \overbrace{u_m(\mathbf{r})u_i(\mathbf{r})} - jk_i p(\mathbf{k}) - \nu k^2 u_i(\mathbf{k})$$

Time advance (e.g., Euler's scheme)

$$u_i(\mathbf{k}, t + dt) = u_i(\mathbf{k}) + dt \times \text{RHS}_i(\mathbf{k}, t)$$

Stiff equation for small viscosity  $\nu$  (use exponential trick)

Nonlinear terms computation:



(pseudo-spectral)

Fourier transforms take around 80% of total time.

Tarang = wave (Sanskrit)

Spectral code (Orszag)

One code to do many  
turbulence & instabilities problems

**VERY HIGH RESOLUTION (6144<sup>3</sup>)**

Cores: 196692 of Shaheen II of KAUST

Open source, download from  
<http://turbulencehub.org>

Chatterjee et al., JPDC 2018

Fluid

MHD, Dynamo

Scalar

Rayleigh-Bénard convection

Stratified flows

Rayleigh-Taylor flow

Liquid metal flows

Rotating flow

Rotating convection

Periodic BC

Free-slip BC

Instabilities

Chaos

Turbulence

No-slip BC

Cylinder

sphere

Toroid

(in progress)



Rich libraries to compute

Spectrum

Fluxes

Shell-to-shell transfer

Structure functions

New things

Fourier modes

Real space probes

Ring-spectrum

Ring-to-ring transfer

Tested up to  $6144^3$  grids

# Object-oriented design

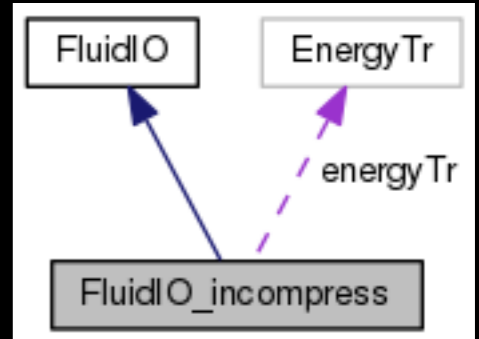
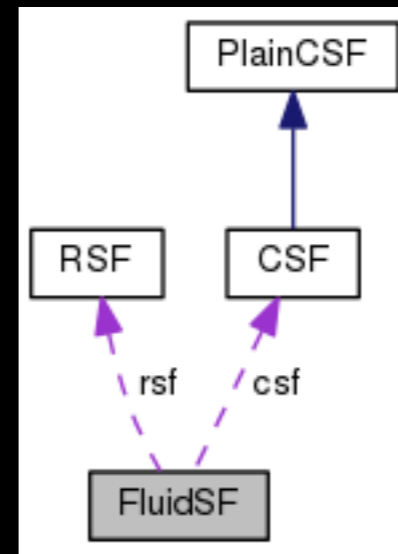
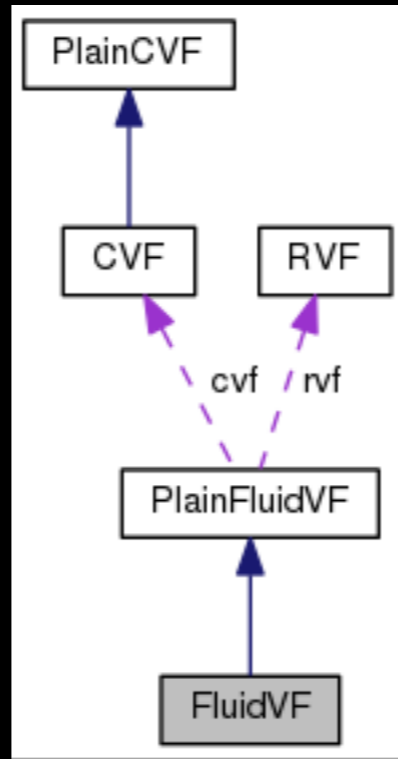
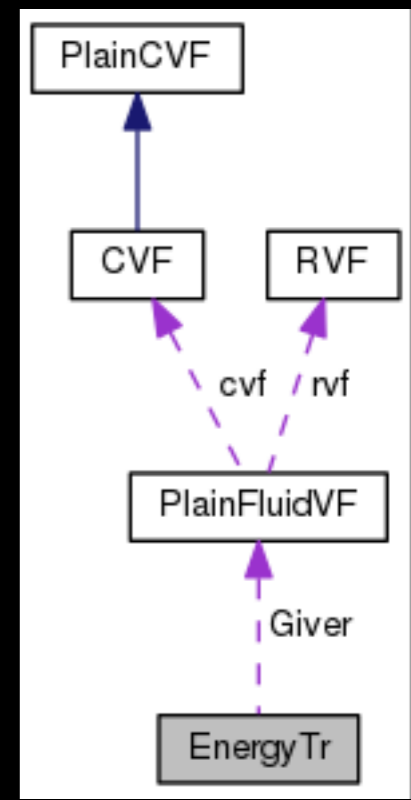
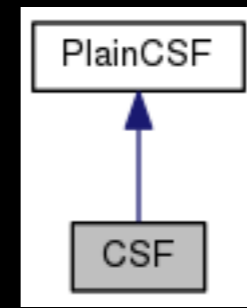
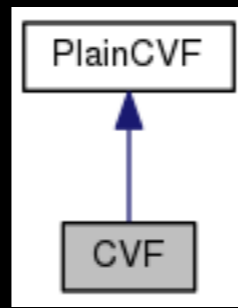
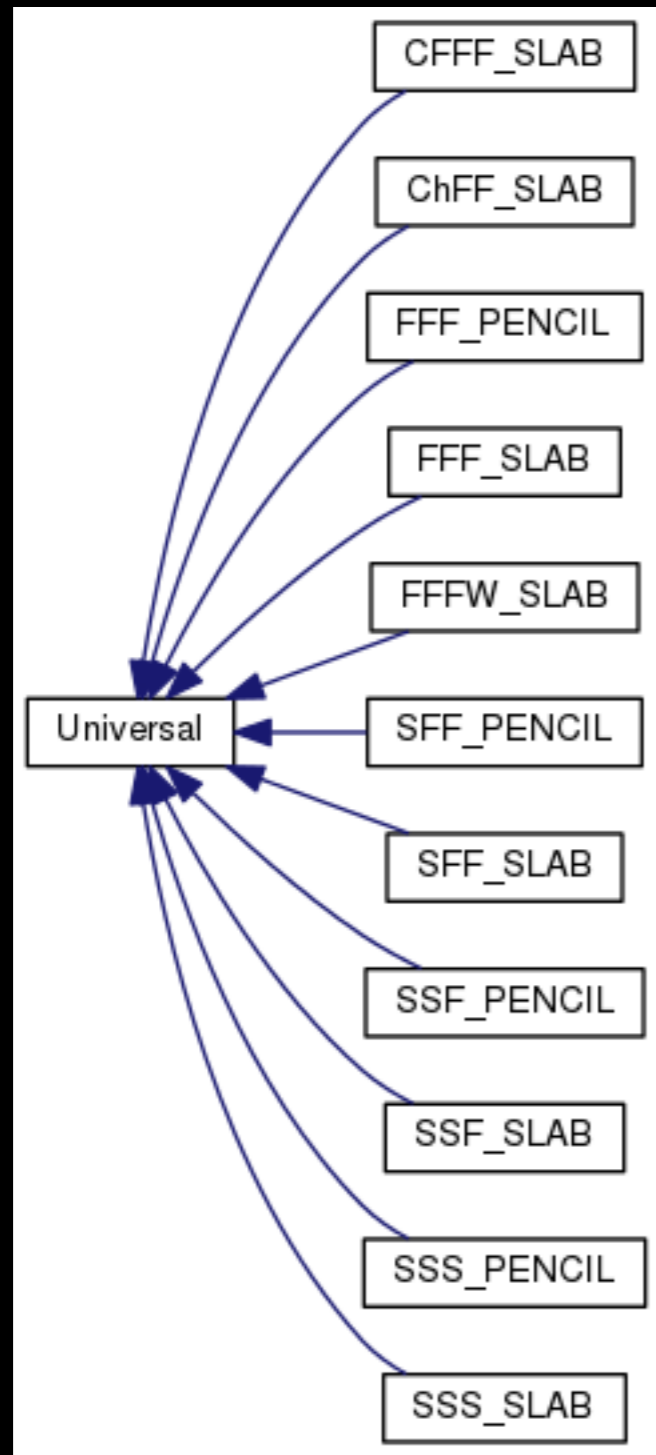
Basis functions (FFF, SFF, SSF, SSS, ChFF)

Basis-independent universal function (function overloading)

e.g., `compute_nlin` ( $u \cdot \nabla$ ) $u$ ,  
( $b \cdot \nabla$ ) $u$ , ( $b \cdot \nabla$ ) $b$ , ( $u \cdot \nabla$ ) $T$ .

General PDE solver

We can use these general functions to simulate  
MHD, convection etc.



Generated by Doxygen

# Parallelization

Spectral Transform  
(FFT, SFT, Chebyshev)

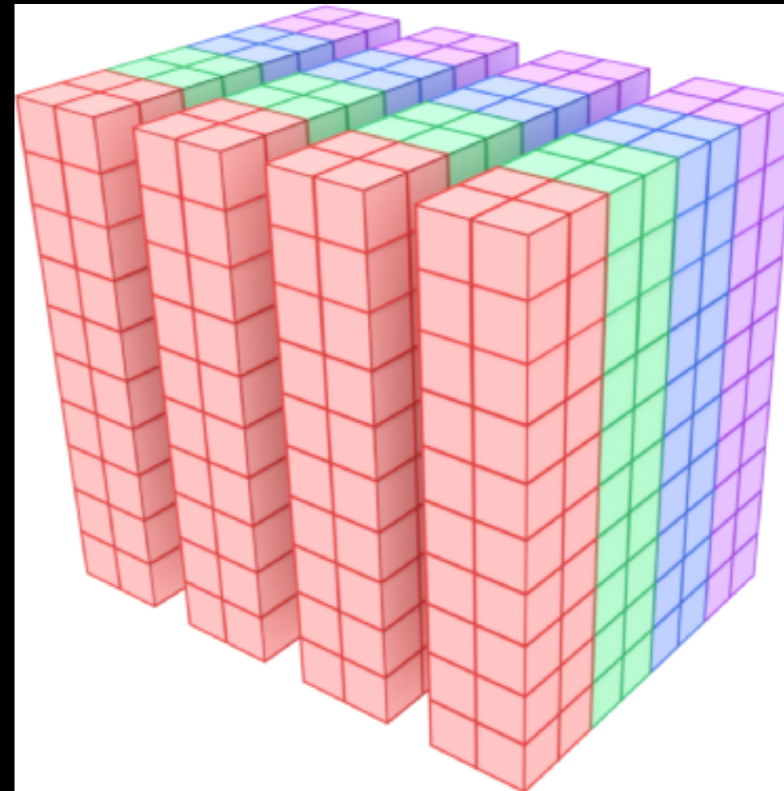
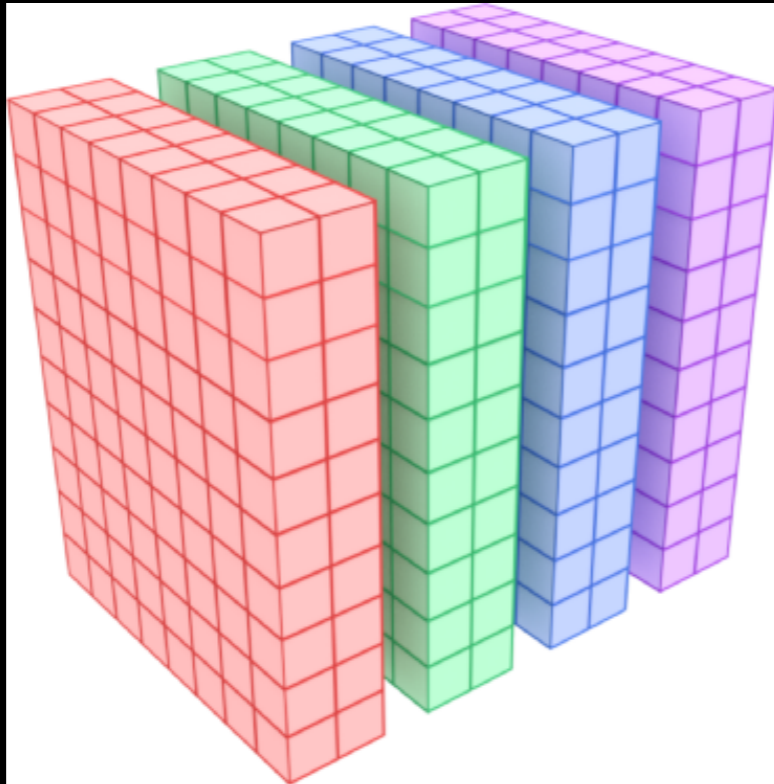
Multiplication in real space

Input/Output  
HDF5 lib

# FFT Parallelization

$$f(x, y, z) = \sum_{k_x} \sum_{k_y} \sum_{k_z} \hat{f}(k_x, k_y, k_z) \exp[i(k_x x + k_y y + k_z z)]$$

# Slab decomposition



Data divided among 4 procs



# Transpose-free FFT

MPI vector, consecutive data transfer

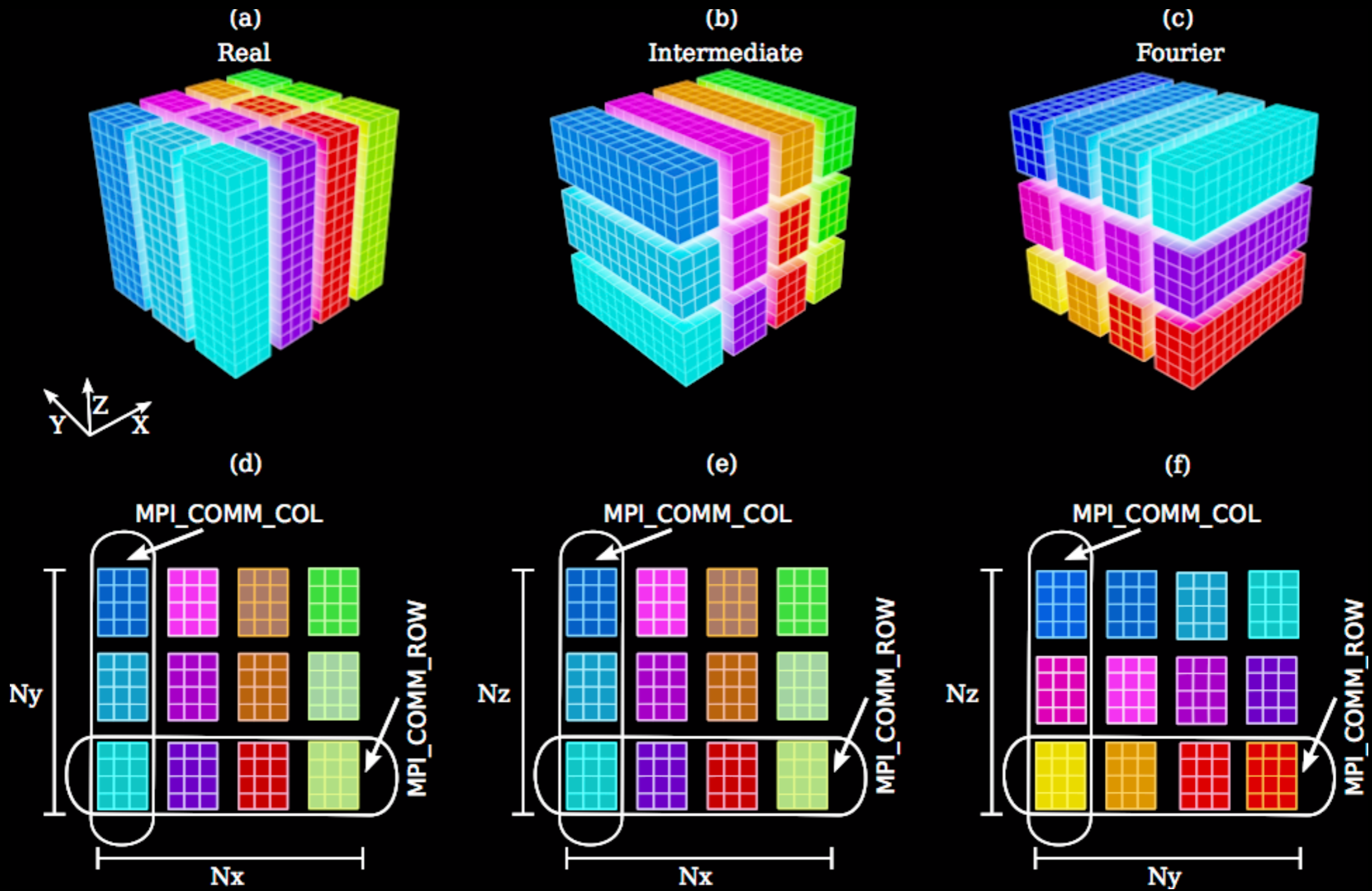
		p0		p1	
p0	1	2	3	4	
	5	6	7	8	
p1	9	10	11	12	
	13	14	15	16	

	p0		p1	
1	2	3	4	
5	6	7	8	
9	10	11	12	
13	14	15	16	

12-15% faster compared to FFTW

# Pencil decomposition

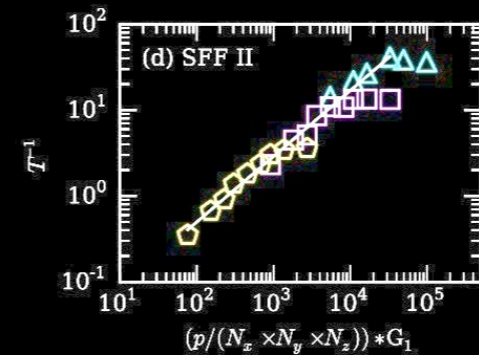
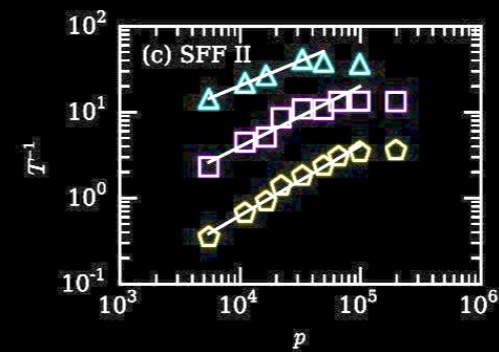
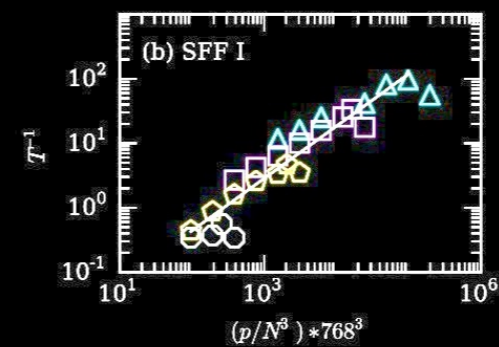
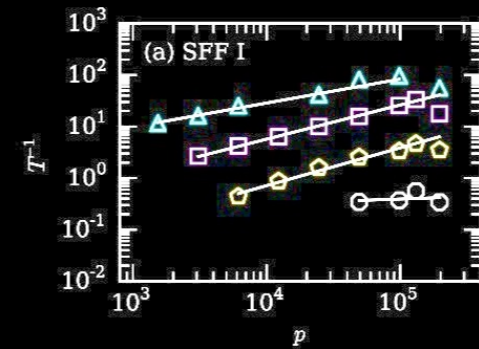
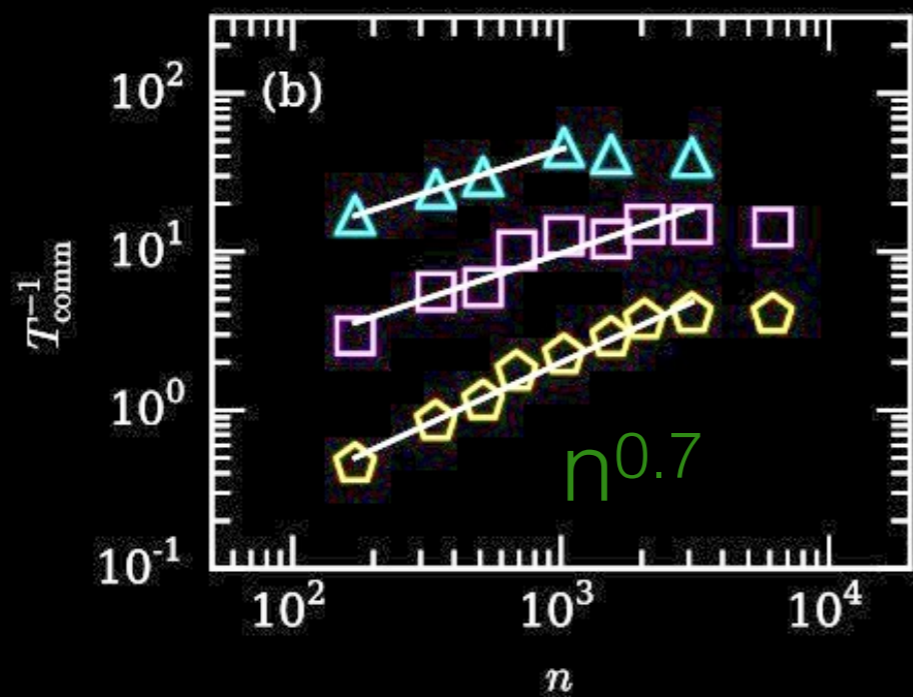
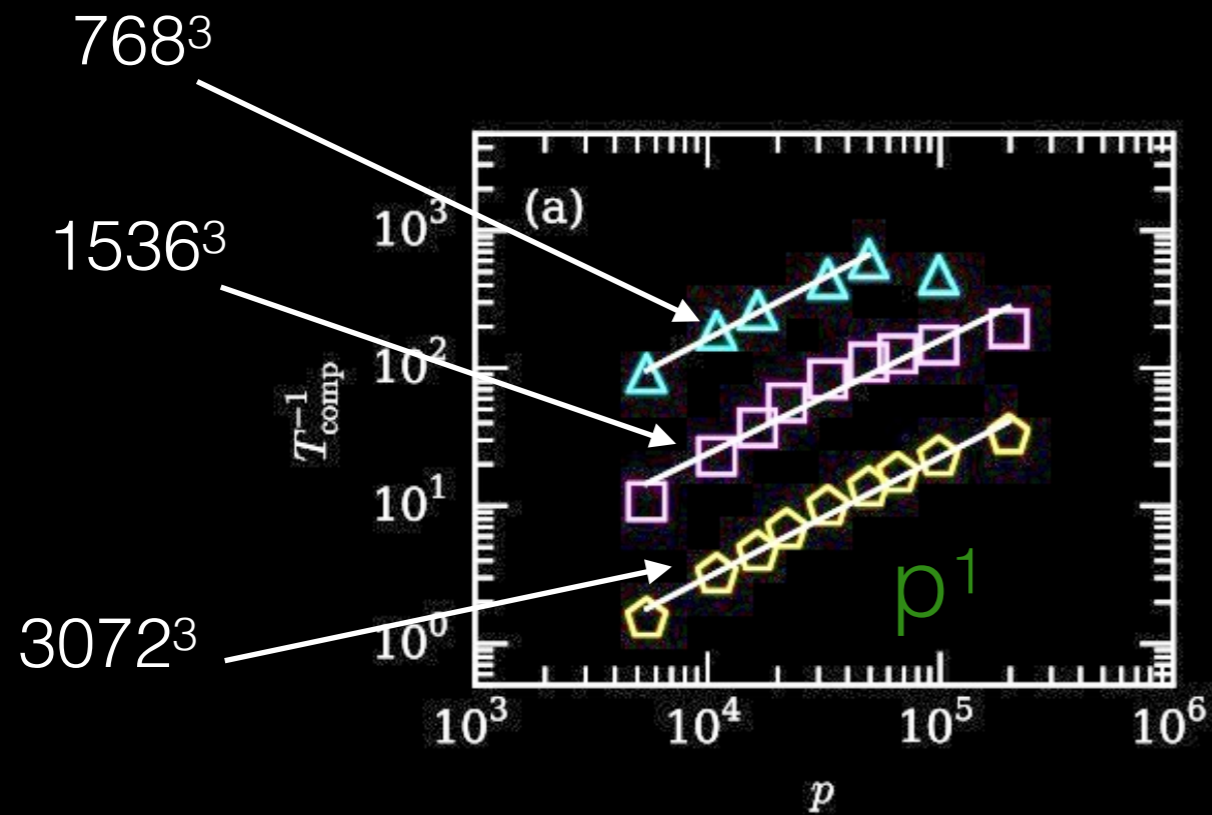


# FFT scaling

On Shaheen 2 at KAUST  
with Anando Chatterjee, Abhishek Kumar,  
Ravi Samtaney, Bilel Hadri, Rooh Khurram

Cray XC40  
ranked 9th in top500

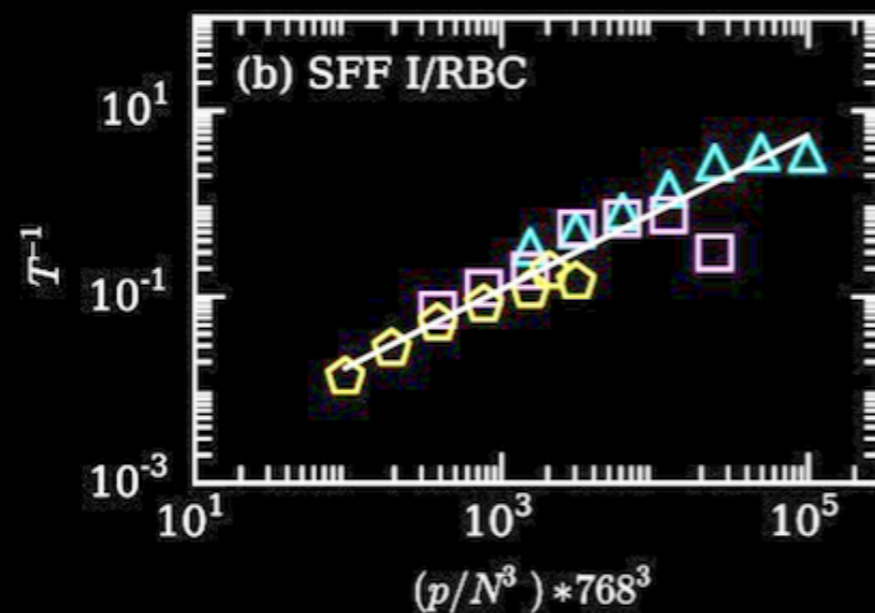
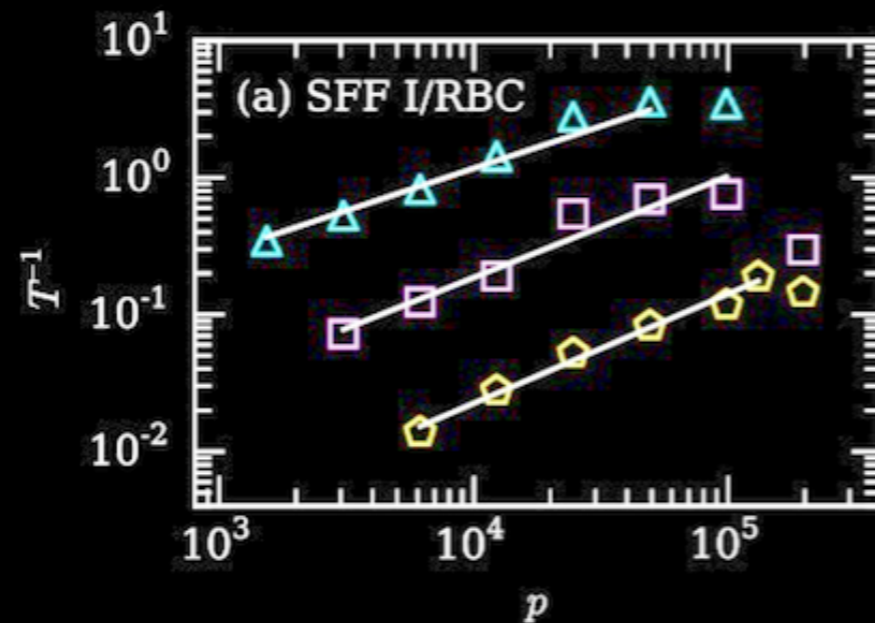
Chatterjee et al., JPDC 2018



# Tarang scaling

On Shaheen at KAUST

- Weak scaling: When we increase the size of the problem, as well as number of procs, then should get the same scaling.



Average flop rating/core (~1.5 %)

Compare with BlueGene/P (~8 %)

Overlap Communication & Computation ??

GPUs ??

Xeon Phi ??

To Petascale &  
then Exascale



# Finite difference code

General code: Easy porting to GPU, MiC

Collaborators:

Roshan Samuel

Fahad Anwer (AMU)

Ravi Samtaney (KAUST)

# Summary

- ★ Code development
- ★ Module development
- ★ Optimization
- ★ Porting to large number of processors
- ★ GPU Porting
- ★ Testing

# Acknowledgements

## **Students:**

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Mani Chandra

Sumit Kumar & Vijay

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Ravi Samtaney

Fahad Anwer

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PARAM, CDAC

Shaheen, KAUST

HPC system IITK

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Dept of Science and Tech., India

Dept of Atomic Energy, India

KAUST (computer time)

Thank you!